

ARTIFICIAL LEARNING CLASSIFIERS WITH  
THE POTENTIAL FUNCTIONS. AN APPROACH  
OF THE GENERAL CASE

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**Abstract:** One of the most important applications of the neural networks is in statistical classification theory. In the specialized literature are procedures which use the artificial process of intelligent machines learning [5]. The Potential Functions Method for two classes is one of them. This paper presents an extension of Potential Functions Method. Our procedure is suitable for the general case when the data set has many classes. We start from the classical method for  $n = 2$  classes and then we provide a procedure for  $n \geq 3$ .

**Key Words:** neural network, classification, potential functions

### 1. Introduction

The powerful learning and the adaptation capability made the neural networks to be very useful. There are many fields, such as decision-making, image processing, insurance, classification and so, that use the neural networks procedures [2, 3, 4].

The Potential Function (P.F.) Method is one of the methods used for training the artificial learning classifiers. The objective is to find the rules which establish a certain class for a new object. For this aim the procedure works on a learning set  $x^1, x^2, \dots, x^p$ , where

$$x^i = (x_1^i, x_2^i, \dots, x_d^i), \quad x^i \in R^d.$$

These data are structured in  $A_1, A_2, \dots, A_n$  linear separable classes,  $A_i \in R^d$ .

The learning sequence is  $(x^n)_{n>0}$ , where each vector is taken infinite times.

The following section is a brief description of Potential Method for two classes. We introduce the basic notation and principles related to this procedure. In Section 3 we offer an extension of the two classes case to the  $n$  classes case and finally we make some conclusions and suggest few directions for further research in this domain.

## 2. Learning Rule with the Potential Method for Two Classes. Notations and Definitions

**Definition 1.** In physics, a potential function  $K : R^d \rightarrow R$  which associates each point  $x$  with the potential in it where this potential is generated by the unit of charge placed in  $x^0$  is:

$$K(x) = \frac{q}{4\pi\epsilon_0 \|x - x^0\|}.$$

**Definition 2.** Generally, a potential function  $K : R^d \times R^d \rightarrow R$  is:

$$K(x, x^k) = \frac{c}{\|x - x^k\|},$$

where  $c$  is a constant.

**Definition 3.** The potential function generated by  $p$  charges  $K : R^d \rightarrow R$  is:

$$K(x) = \sum_{k=1}^p q_k K(x, x^k),$$

where  $q_k$  is the charge placed in  $x^k$ .

The potential learning method for two classes  $A_1, A_2$  and for learning set  $x^1, x^2, \dots, x^p$  uses a potential function as decision function:

$$g(x) = K(x).$$

In each points which are in  $A_1$  is placed a positive unit charge and in each points which are in  $A_2$  is placed a negative one. The electric potential of class  $A_1$  is positive and the potential of class  $A_2$  is negative.

The P.F. procedure starts with a decision function  $K(x)$  then the vectors of learning set are treated one by one.

This method is a training method based on error correction. The potential is corrected by modifying the value of  $q_j$  in case of incorrect classification for the object  $x^j$ . If  $x^j$  is in  $A_1$  set and it is incorrect classified in  $A_2$  then the potential is increased by adding one unit of charge to  $q_j$ . If  $x^j$  is in  $A_2$  and is incorrect classified in  $A_1$  then the potential is decreased by taking a unit of charge from  $q_j$ . In case of a correct classification the potential remain unmodified.

Dumutrescu [1] described the previous procedure in the following algorithm:

$$K_{k+1}(x) = \begin{cases} K_k(x) + K(x, x^{k+1},) & \text{if } x^{k+1} \in A_1 \text{ and } K_k(x^{k+1}) \leq 0, \\ K_k(x) - K(x, x^{k+1}), & \text{if } x^{k+1} \in A_2 \text{ and } K_k(x^{k+1}) \geq 0, \\ K_k(x), & \text{if } x^{k+1} \in A_1 \text{ and } K_k(x^{k+1}) > 0, \\ & \text{or if } x^{k+1} \in A_2 \text{ and } K_k(x^{k+1}) < 0. \end{cases}$$

### 3. An Algorithm which Uses the Potential Method for $n$ Classes

Let  $A_1, A_2, \dots, A_n$  classes, with  $n \geq 3$  and  $x^1, x^2, \dots, x^p$  the learning set. In this case we have  $n$  decision functions which must be founded:

$$g_{ik} : R^d \rightarrow R, \quad i = 1, \dots, n,$$

and  $k$  denote the procedure stage.

The decision functions will be the potential functions:

$$g_{ik} = K_k^i.$$

For the general case when the classes number is bigger then two, we give the following rule for change the decision functions. So, we obtain a sequence which converge to the optimal decision functions.

Let  $q_1, q_2, \dots, q_p$  the charges placed at random in  $x^1, x^2, \dots, x^p$ , then:

$$K_{k+1}^r(x) = \begin{cases} K_k^i(x) + K(x, x^{k+1},) & \text{if } r = i \text{ and } K_k^i(x^{k+1}) \leq K_k^j(x^{k+1}), \\ K_k^j(x) - K(x, x^{k+1}), & \text{if } r = j \text{ and } K_k^i(x^{k+1}) \geq K_k^j(x^{k+1}), \\ K_k^t(x), & \text{if } r = t, t \neq i, j, K_k^i(x^{k+1}) > K_k^t(x^{k+1}), \\ & t = 1, \dots, n. \end{cases}$$

where  $K_{k+1}^i$  is the  $i$ -th class potential at the  $k$ -stage and  $x^k$  is the learning vector presented at the  $k$ -stage.

#### 4. Conclusions and Possible Future Directions

The purpose of this paper is to give a Potential Functions procedure for general case. Thus we will dispose of a new procedure for artificial learning classifiers. In practical classification application this method may be compared with the existent methods or may replaces one of them.

The P.F. method for  $n$  classes can be helpfully when the learning set  $R^2$  has a small number of elements or when the space has a small dimension.

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